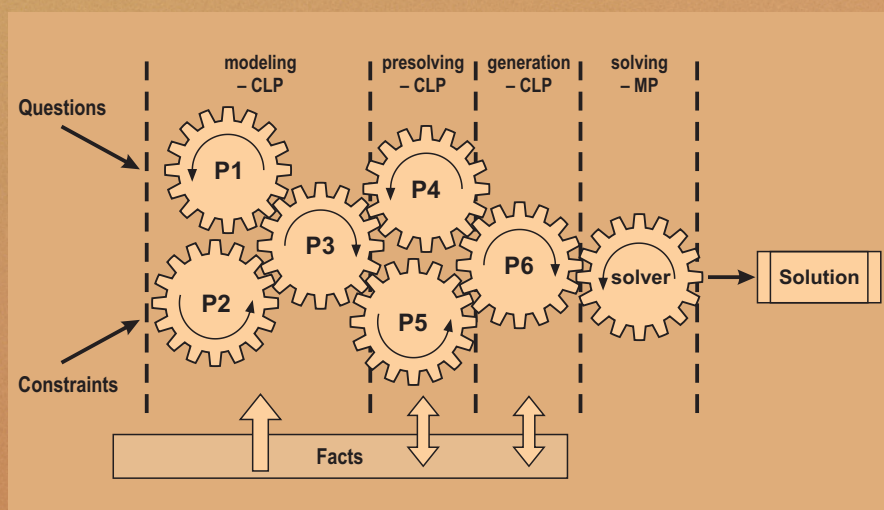


Paweł Sitek

A HYBRID APPROACH TO MODELING AND SOLVING DISTRIBUTION PROBLEMS



MONOGRAFIE, STUDIA, ROZPRAWY

M98

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